

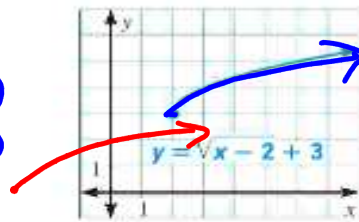
Warm Up

*Need Graph Paper

VOCABULARY CHECK

Copy and complete the statement using the graph at the right.

1. The **domain** of the function is $(2, \infty)$
2. The **range** of the function is $(3, \infty)$
3. The **inverse** of the function is $Y = (x-3)^2 + 2$



SKILLS CHECK

Graph the function. State the domain and range. (Review p. 446 for 7.1-7.3.)

- | | | |
|-------------------------|---|--|
| 4. $y = -2\sqrt{x} - 1$ | 5. $y = \sqrt{x+3}$ $(-3, \infty)$ $(0, \infty)$ | 6. $y = \sqrt[3]{x-2} + 5$ $(-\infty, \infty)$ |
|-------------------------|---|--|

Find the inverse of the function. (Review p. 438 for 7.4.)

- | | | |
|-----------------|--------------------|-----------------------------------|
| 7. $y = 3x + 5$ | 8. $y = -2x^3 + 1$ | 9. $y = \frac{1}{2}x^2, x \geq 0$ |
|-----------------|--------------------|-----------------------------------|

$$\begin{aligned}
 -x &= -2y^3 + 1 \\
 \frac{-x-1}{-2} &= \frac{-2y^3 + 1 - 1}{-2} \\
 \sqrt[3]{\frac{-x-1}{-2}} &= \sqrt[3]{\frac{-2y^3}{-2}} \\
 Y &= \sqrt[3]{\frac{-x-1}{-2}}
 \end{aligned}$$

A

$$\begin{aligned}
 \textcircled{11} & -5\sqrt[3]{16} + 2\sqrt[3]{28} \\
 & -5\sqrt[3]{8 \cdot 2} + 2\sqrt[3]{64 \cdot 2} \\
 & -5 \cdot 2\sqrt[3]{2} + 2 \cdot 4\sqrt[3]{2} \\
 & -10\sqrt[3]{2} + 8\sqrt[3]{2} \\
 & -2\sqrt[3]{2}
 \end{aligned}$$

B

$$\begin{aligned}
 \textcircled{11} & -5\sqrt[3]{250} + 2\sqrt[3]{6} \\
 & -5\sqrt[3]{125 \cdot 2} + 2\sqrt[3]{8 \cdot 2} \\
 & -5 \cdot 5\sqrt[3]{2} + 2 \cdot 2\sqrt[3]{2} \\
 & -25\sqrt[3]{2} + 4\sqrt[3]{2} \\
 & -21\sqrt[3]{2}
 \end{aligned}$$

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

*What is an exponential function?

$$y = 2 \cdot 3^x$$

$$y = -2 \cdot 3^x$$

$y = ab^x$ where $a \neq 0$ and the base b is a positive number other than 1.

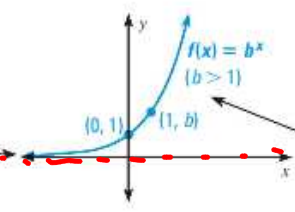
*If $a > 0$ and $b > 1$, the function $y = ab^x$ is an exponential growth function, and b is called the growth factor.

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

KEY CONCEPT *For Your Notebook*

Parent Function for Exponential Growth Functions

The function $f(x) = b^x$, where $b > 1$, is the parent function for the family of exponential growth functions with base b . The general shape of the graph of $f(x) = b^x$ is shown below.



The x-axis is an **asymptote** of the graph. An asymptote is a line that a graph approaches more and more closely.

The graph rises from left to right, passing through the points $(0, 1)$ and $(1, b)$.

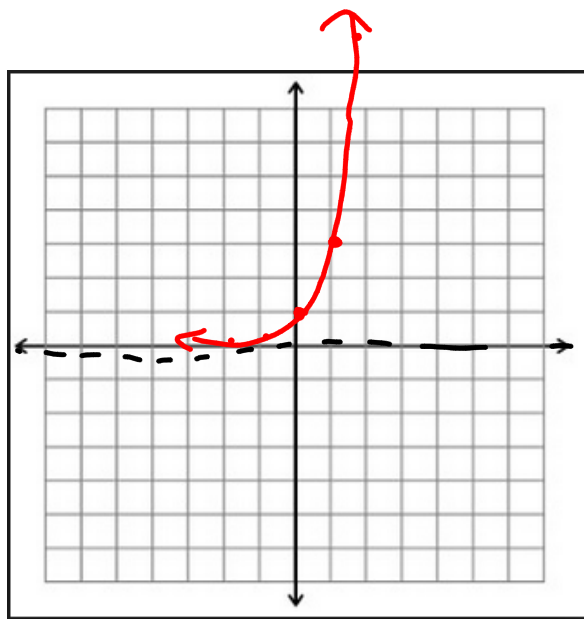
The domain of $f(x) = b^x$ is all real numbers. The range is $y > 0$.

$y = 2 \cdot 3^x + 4$

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

Graph $y=3^x$ $D: (-\infty, \infty)$ $R: (0, \infty)$ Steps to graphing:

- 1) Make a table of values.
- 2) Plot the points from the table.
- 3) Draw the curve.



| x | y |
|-----|------------------------|
| -2 | $3^{-2} = \frac{1}{9}$ |
| -1 | $3^{-1} = \frac{1}{3}$ |
| 0 | $3^0 = 1$ |
| 1 | $3^1 = 3$ |
| 2 | $3^2 = 9$ |

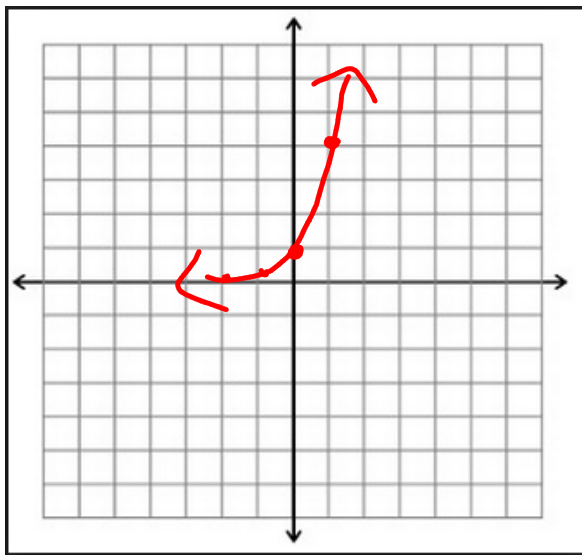
7.1 & 7.2 Graphing Exponential Growth & Decay
 TOYO Functions

Graph $y=4^x$ $D: (-\infty, \infty)$ Steps to graphing:

$R: (0, \infty)$ 1) Make a table of values.

2) Plot the points from the table.

3) Draw the curve.



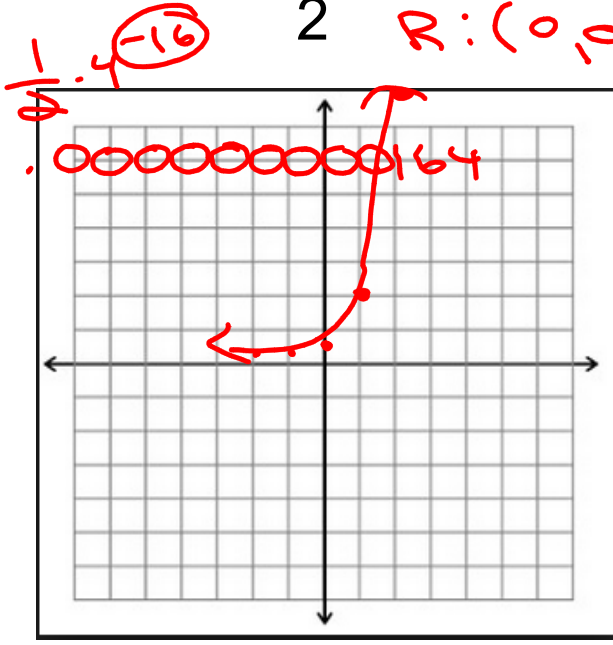
| X | Y |
|----|-------------------------|
| -2 | $4^{-2} = \frac{1}{16}$ |
| -1 | $4^{-1} = \frac{1}{4}$ |
| 0 | $4^0 = 1$ |
| 1 | $4^1 = 4$ |
| 2 | $4^2 = 16$ |

7.1 & 7.2 Graphing Exponential Growth & Decay Functions
TOYO

Graph $y = \frac{1.4^x}{2}$ D: $(-\infty, \infty)$ R: $(0, \infty)$

Steps to graphing:

- 1) Make a table of values.
- 2) Plot the points from the table.
- 3) Draw the curve.



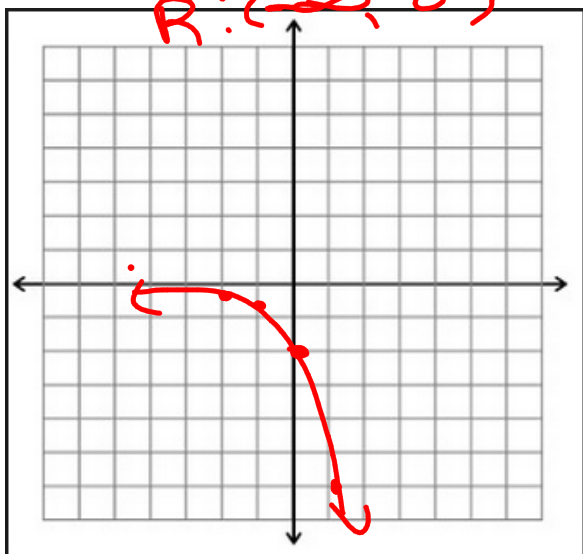
| x | y |
|----|-------|
| -2 | 0.175 |
| -1 | 0.35 |
| 0 | 0.5 |
| 1 | 0.7 |
| 2 | 1.0 |

*Spring Break Fun?

$$y = -2 \cdot 3^x$$

$$D: (-\infty, \infty)$$

$$R: (-\infty, 0)$$



| x | y |
|----|---|
| -2 | $-2 \cdot 3^{-2} = -2 \cdot \frac{1}{9} = -\frac{2}{9}$ |
| -1 | $-2 \cdot 3^{-1} = -2 \cdot \frac{1}{3} = -\frac{2}{3}$ |
| 0 | $-2 \cdot 3^0 = -2 \cdot 1 = -2$ |
| 1 | $-2 \cdot 3^1 = -2 \cdot 3 = -6$ |
| 2 | $-2 \cdot 3^2 = -2 \cdot 9 = -18$ |

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

What is the y-intercept of the graph $y=ab^x$?

$(0,a)$

Ex: Find the y-intercept of $y= \frac{1.2^x}{4}$.

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

Translations:

$$y = ab^{x-h} + k$$

Left/Right (with arrow pointing to h)
up/down (with arrow pointing to k)

1) Graph $y = ab^x$

2) Translate the graph horizontally by h units and vertically by k units.

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

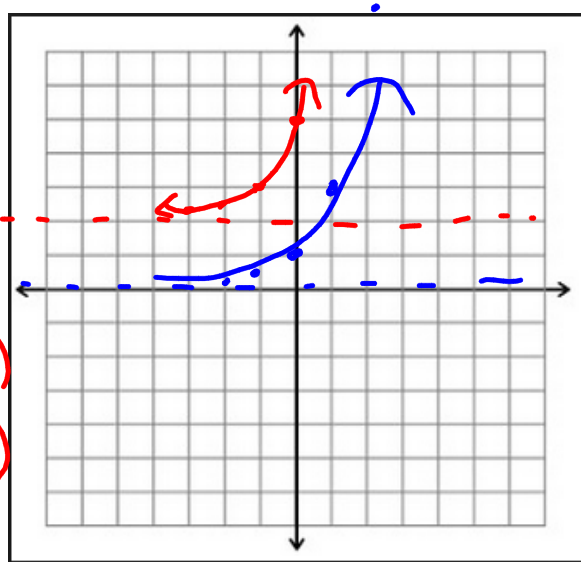
Graph: $y = 3^{x+1} + 2$

State the domain and range

$y = 3^x$

| X | Y |
|----|-----|
| -2 | 1/9 |
| -1 | 1/3 |
| 0 | 1 |
| 1 | 3 |
| 2 | 9 |

Range
 left + one up 2
 D: $(-\infty, \infty)$
 R: $(2, \infty)$



- 1) Graph $y = ab^x$
- 2) Translate the graph horizontally by h units and vertically by k units.

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

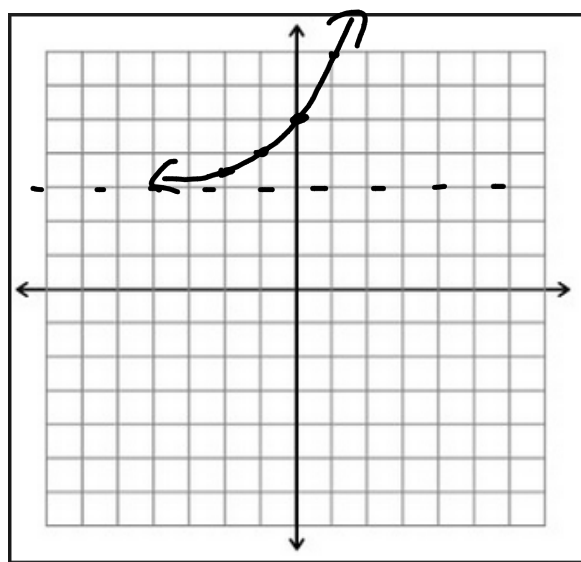
TOYO

Graph: $y = 2^{x+1} + 3$

State the domain and range.

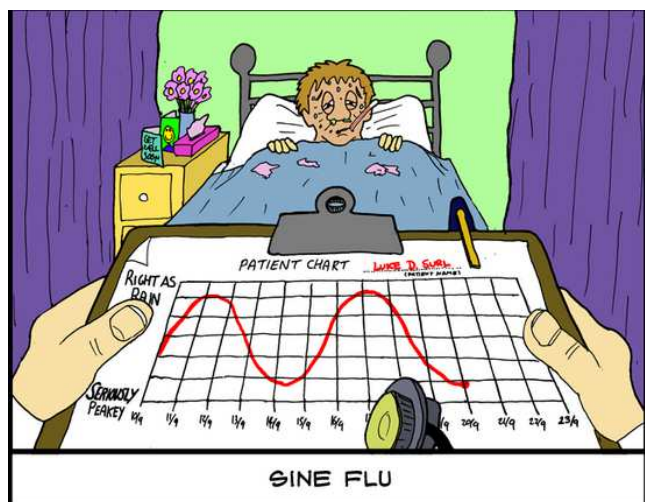
| X | Y |
|----|-----|
| -2 | 3.5 |
| -1 | 4 |
| 0 | 5 |
| 1 | 7 |

$D: (-\infty, \infty)$
 $R: (3, \infty)$



1) Graph $y = ab^x$

2) Translate the graph horizontally by h units and vertically by k units.



Happy Face Math

| | |
|-----------------------------------|---|
| $\text{😊}^{-1} = \text{😞}$ | $\text{Re}(\text{😊}) = \text{😊}$ No i's |
| $\text{😊}^2 = \text{😊}^2$ | $\text{Im}(\text{😊}) = \dots$ |
| $\text{😊}^3 = \text{😊}^3$ | $\nabla \chi(\text{😊}) = \text{😊}$ |
| $\text{sup}(\text{😊}) = \text{😊}$ | $\nabla(\text{😊}) = \text{😊}$ |
| $\partial(\text{😊}) = \text{😊}$ | $\log(\text{😊}) = \text{😊}$ |
| $\text{sin}(\text{😊}) = \text{😊}$ | |

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

What is the y-intercept of the graph $y=ab^x$?

$(0,a)$

Ex: Find the y-intercept of $y=-(5/2)^x$.

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

Exponential decay functions-

$$y=ab^x \text{ where } a>0 \text{ and } 0<b<1$$

The base b of an exponential decay function is called the ~~decay factor~~.

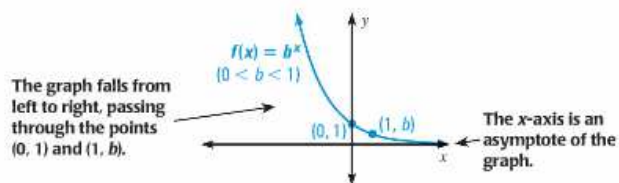
7.1 & 7.2 Graphing Exponential Growth & Decay Functions

KEY CONCEPT

For Your Notebook

Parent Function for Exponential Decay Functions

The function $f(x) = b^x$, where $0 < b < 1$, is the parent function for the family of exponential decay functions with base b . The general shape of the graph of $f(x) = b^x$ is shown below.



The domain of $f(x) = b^x$ is all real numbers. The range is $y > 0$.

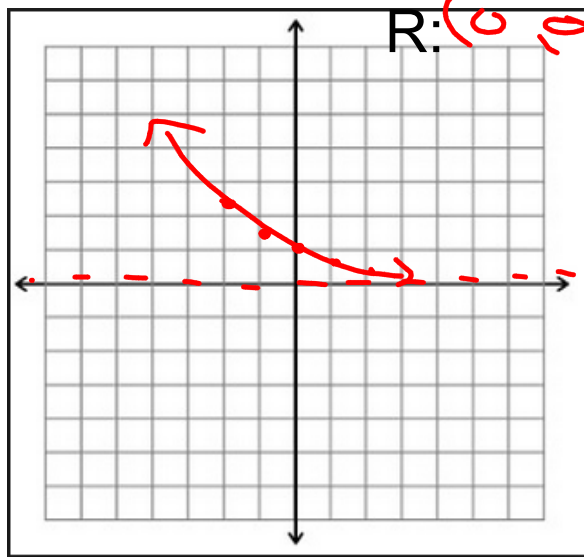
7.1 & 7.2 Graphing Exponential Growth & Decay Functions

Graph $y = (2/3)^x$

D: $(-\infty, \infty)$
 R: $(0, \infty)$

Steps to graphing:

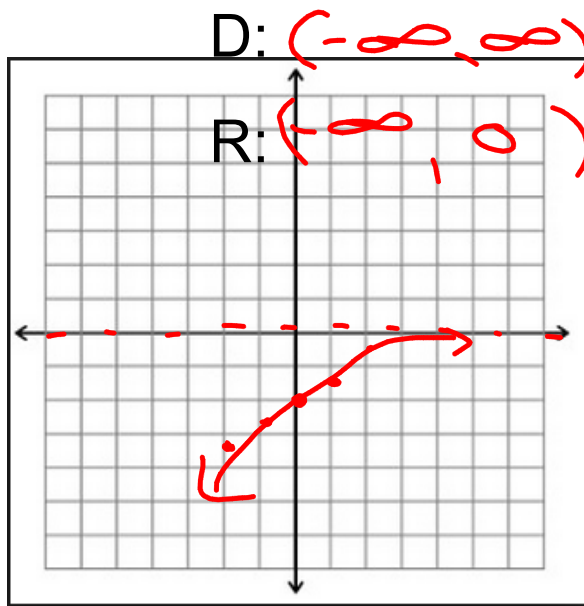
- 1) Make a table of values.
- 2) Plot the points from the table.
- 3) Draw the curve.



| x | y |
|----|---|
| -2 | $(\frac{2}{3})^{-2} = (\frac{3}{2})^2 = \frac{9}{4} = 2\frac{1}{4}$ |
| -1 | $(\frac{2}{3})^{-1} = \frac{3}{2}$ |
| 0 | 1 |
| 1 | $\frac{2}{3}$ |
| 2 | $\frac{4}{9}$ |

7.1 & 7.2 Graphing Exponential Growth & Decay Functions
TOYO

Graph $y = -2(3/4)^x$



Steps to graphing:

- 1) Make a table of values.
- 2) Plot the points from the table.
- 3) Draw the curve.

| X | Y |
|----|---|
| -2 | $-2 \cdot \frac{3^2}{4^2} = -\frac{3}{2}$ |
| -1 | $-2 \cdot \frac{3^1}{4^1} = -\frac{3}{2}$ |
| 0 | $-2 \cdot 1 = -2$ |
| 1 | $-2 \cdot \frac{3}{4} = -\frac{3}{2}$ |
| 2 | $-2 \cdot \frac{9}{16} = -\frac{9}{8}$ |

7.1 & 7.2 Graphing Exponential Growth & Decay Functions

✓ **GUIDED PRACTICE** for Examples 3 and 4

Graph the function. State the domain and range.

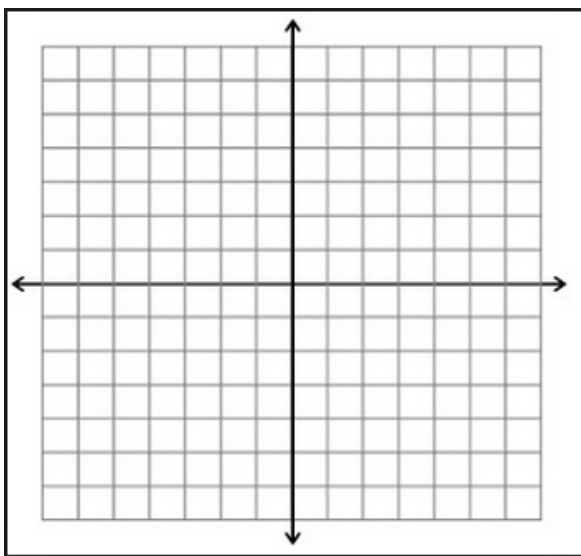
4. $y = \left(\frac{1}{4}\right)^{x-1} + 1$

5. $y = 5\left(\frac{2}{3}\right)^{x+1} - 2$

6. $g(x) = -3\left(\frac{3}{4}\right)^{x-5} + 4$

TOYO

5&6



How can you tell the difference between growth and decay?

$$y = ab^{x+h} + k$$

$$y = -2 \left(\frac{3}{4}\right)^x \quad \text{D}$$

$$y = 3 \cdot \left(\frac{1}{2}\right)^{x+1} - 2 \quad \text{D}$$

$$y = 4 \cdot 2^{x-1} - 3 \quad \text{G}$$

$$y = \left(\frac{1}{2}\right)^x \quad \text{D}$$

$$y = \frac{1}{3} \cdot 4^x \quad \text{G}$$

*Go over test

Homework:

Page 482 #6-21 multiples of 3

Page 489 #3-6, 9-24 multiples of 3, 25